

**Mathcad sheet to derive U for SW with GBN**

$f(i) := 1 + (i - 1) \cdot K$       Number of packets to be sent for try i

$N := \sum_{i=1}^{\infty} [f(i) \cdot p^{i-1} \cdot (1-p)]$       We need to solve for N symbolically

$N := (1-K)(1-p) \cdot \sum_{i=1}^{\infty} p^{i-1} + K \cdot (1-p) \cdot \sum_{i=1}^{\infty} (i \cdot p^{i-1})$       Step #1 by hand

$N \rightarrow \begin{cases} (K-1) \cdot (p-1) \cdot \infty - \frac{K}{p-1} & \text{if } 1 \leq p \\ 1 - \frac{K}{p-1} - K & \text{if } p \neq 1 \wedge |p| < 1 \end{cases}$       Here is our result

$U := \frac{W \cdot t_{fr}}{\left(1 - \frac{K}{p-1} - K\right) \cdot (t_{fr} + 2 \cdot t_{pr})}$       So we now have this, but what is K

For W too small to fill the pipe  $K = W$ . We simplify the above to get:

$U := \frac{W \cdot (1-p) \cdot t_{fr}}{(t_{fr} + 2 \cdot t_{pr}) \cdot (W \cdot p + 1 - p)}$       Simplified for case of W too small to fill pipe

For W large enough to fill the pipe  $K = t_{fr} / (t_{fr} + 2t_{pr})$ . We then get:

$U := \frac{1}{\left[1 - \frac{\left(\frac{t_{fr} + 2 \cdot t_{pr}}{t_{fr}}\right)}{p-1} - \left(\frac{t_{fr} + 2 \cdot t_{pr}}{t_{fr}}\right)\right]}$

$U := \frac{(1-p) \cdot t_{fr}}{2 \cdot p \cdot t_{pr} + t_{fr}}$

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